

A Simulative Model for the Analysis of Conduction Properties of Ion Channels Based on First-Principle Approaches

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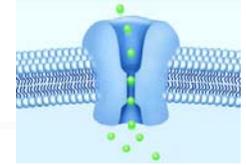


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IWCE-10 Purdue University, West Lafayette, Indiana, USA

Outline



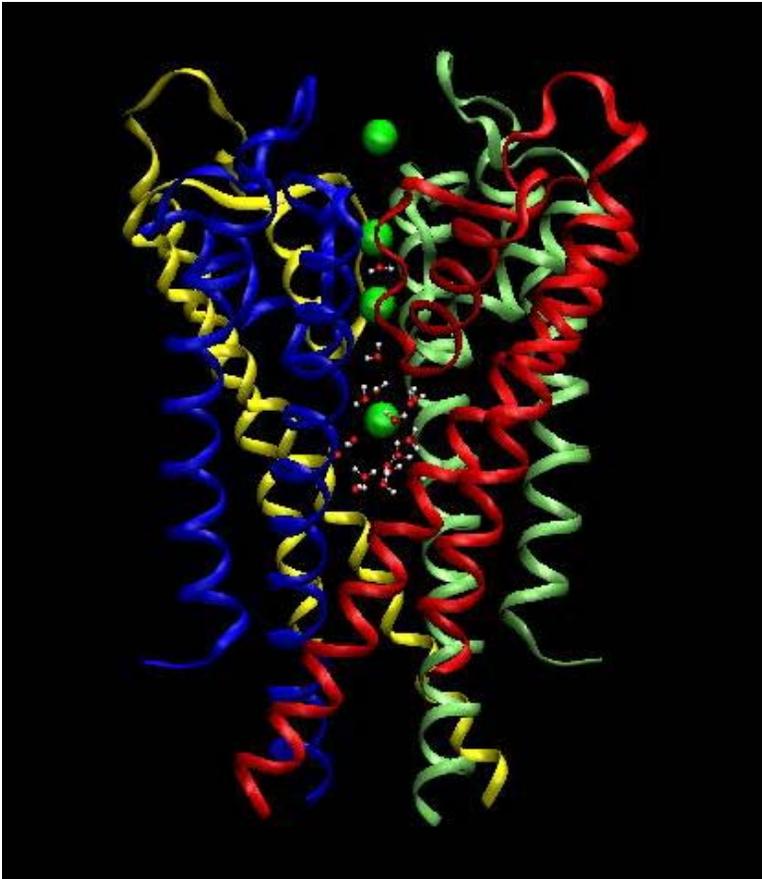
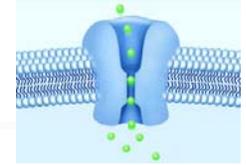
- The problem and our goal
- State of the art
- Our model and simulative procedure
- Results
- Further research developments

Ideas and hints also from:

*M. Cascella, M. Ferrario, J. Kona,
S. Moroni, L. Reggiani, B. Roux, V. Torre*

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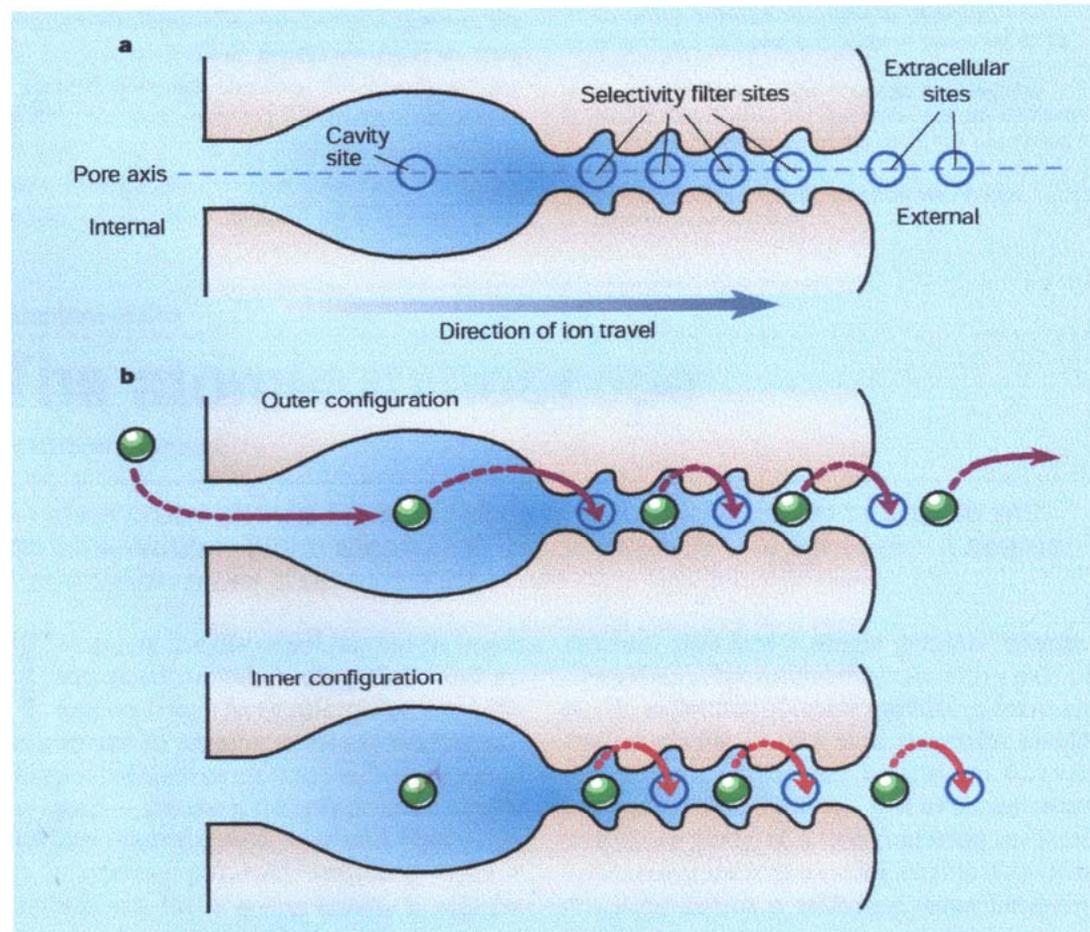
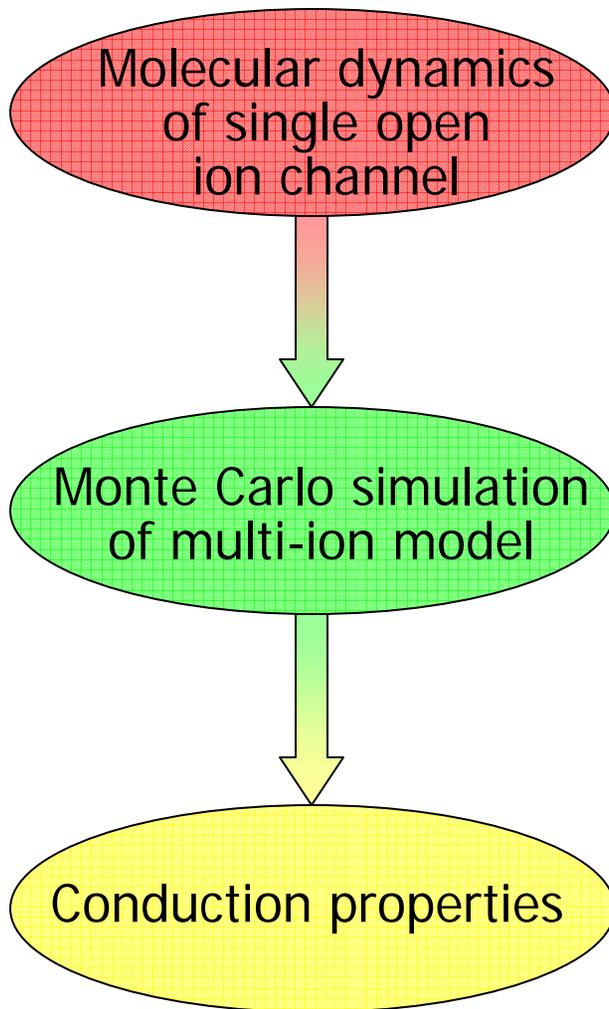
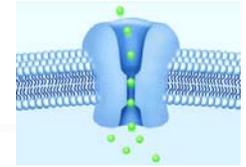
The problem...



VMD snapshot

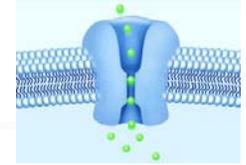
- Ion channels are **nanometric macromolecular pores in cell membranes** formed by proteins
- They have **selective ion conduction** and the ability to gate-open in response to an appropriate stimulus
- Since 1998 **X-ray crystallographic structures**, providing atomic resolution of some channel proteins, have been obtained
- KcsA potassium channel is a good prototype to test any realistic simulative model

... and our goal



From C. Miller, *Nature*, **414** (2001)

State of the art



Experimental scenario

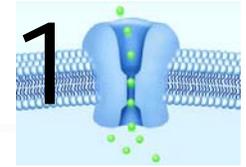
Electrical characterization of single open channels embedded in planar lipid bilayers in presence of buffered solutions with symmetrical K^+ concentration

(see Miller – USA, Schrempf – Germany)

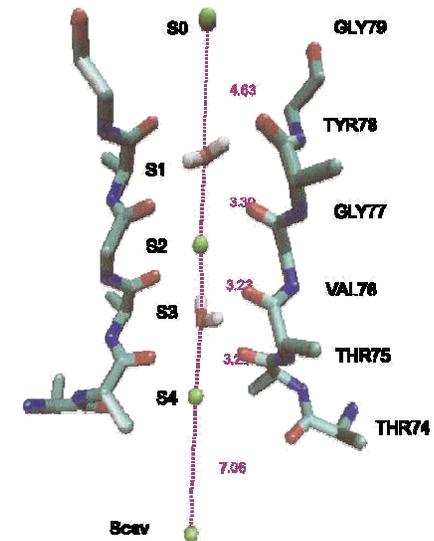
Theoretical models

- ✓ Single-file multi-ion models (e.g. Hille) (since 1970)
- ✓ Continuum Models, e.g. Poisson-Nernst-Planck (PNP) models (e.g. Heisenberg) (since 1970)
- ✓ Atomistic MD simulations and Brownian-Dynamics simulations (e.g. Roux) (since 1988)

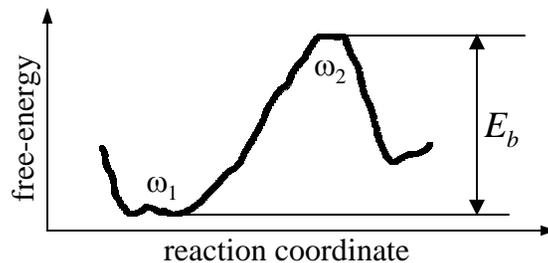
Our simulative procedure... 1



The possible configurations of the channel are defined through the K⁺ occupancy of a set of individual binding sites within the pore ($S_{\text{ext}}, S_0 \dots S_4, S_{\text{cav}}$), identified from structural data and MD simulations, under the hypothesis of single-file concerted motion



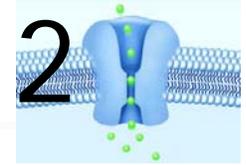
The transition rates can be estimated by calculating the average time a given transition needs to take place from MD or using the Kramers' formula:



$$k_{A \rightarrow B} = \frac{M \omega_1 \omega_2}{2\pi D} e^{-\frac{E_b}{kT}}$$

where the diffusion coefficient D , the energy barrier E_b and the frequency ω_1, ω_2 come directly from MD simulations

Our simulative procedure... 2



The MD approach includes a modified GROMOS87 force-field. The high-resolution (2.0 Å) KcsA protein structure is embedded into a water-octane-water bilayer. A total of 34434 atoms have been considered.

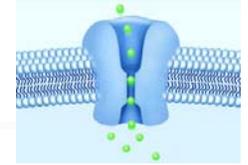
The free-energy difference between the initial and final configurations is evaluated from MD through a multiple-steering dynamics procedure

The ion capture probability assumes an energy barrier of $8 k_B T$ (approx. 5 Kcal/mol) both at intracellular and extracellular reservoirs and has been estimated from the classical kinetic theory of gases:

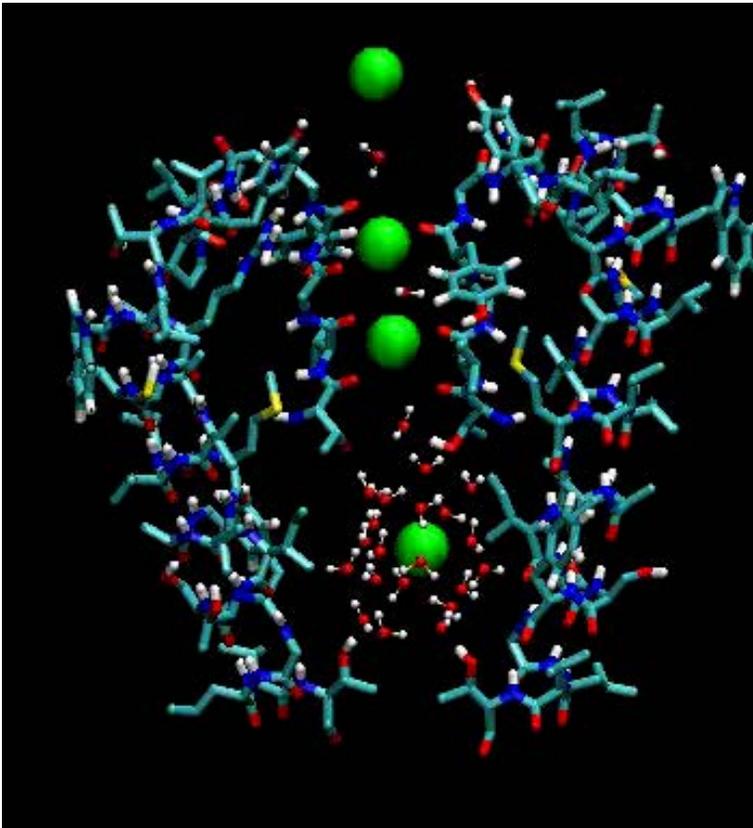
$$k_{\text{entry}} = \frac{n\sigma}{6} \sqrt{\frac{k_B T}{2M}} e^{-\frac{E_{in}}{kT}}$$

Being n the ion concentration and σ the cross sectional area of the vestibule

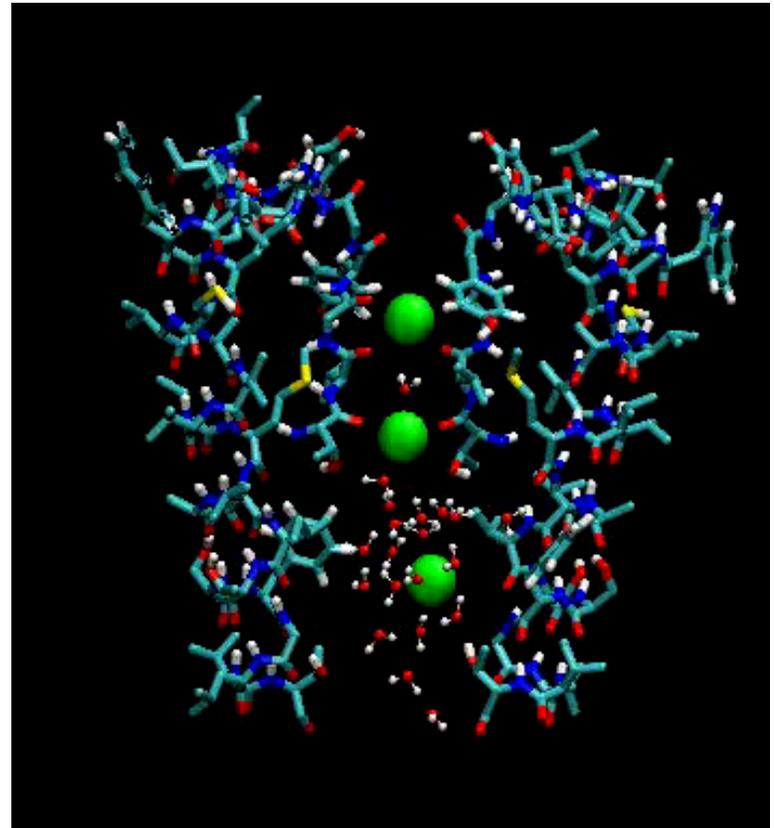
Results



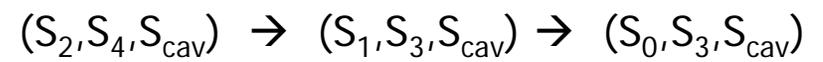
Observed transitions



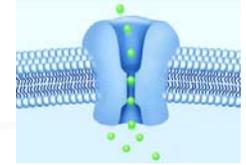
VMD movie



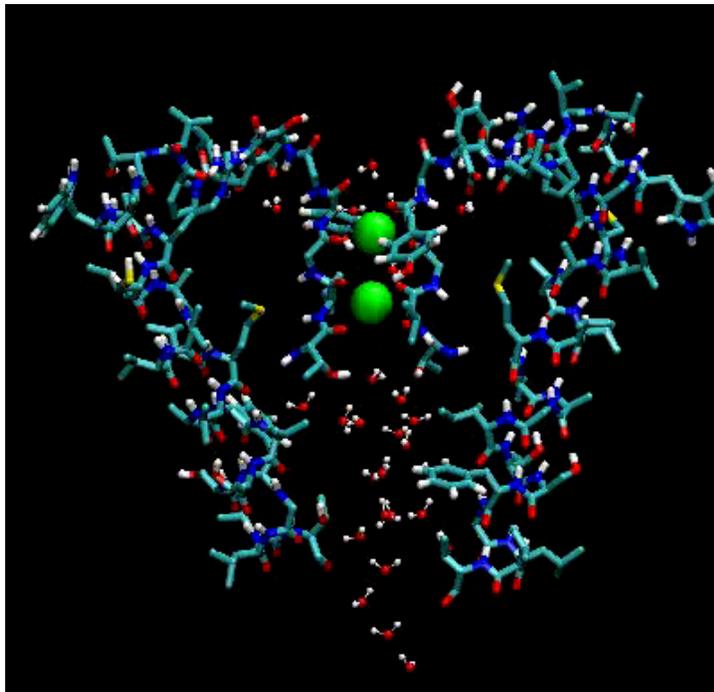
VMD movie



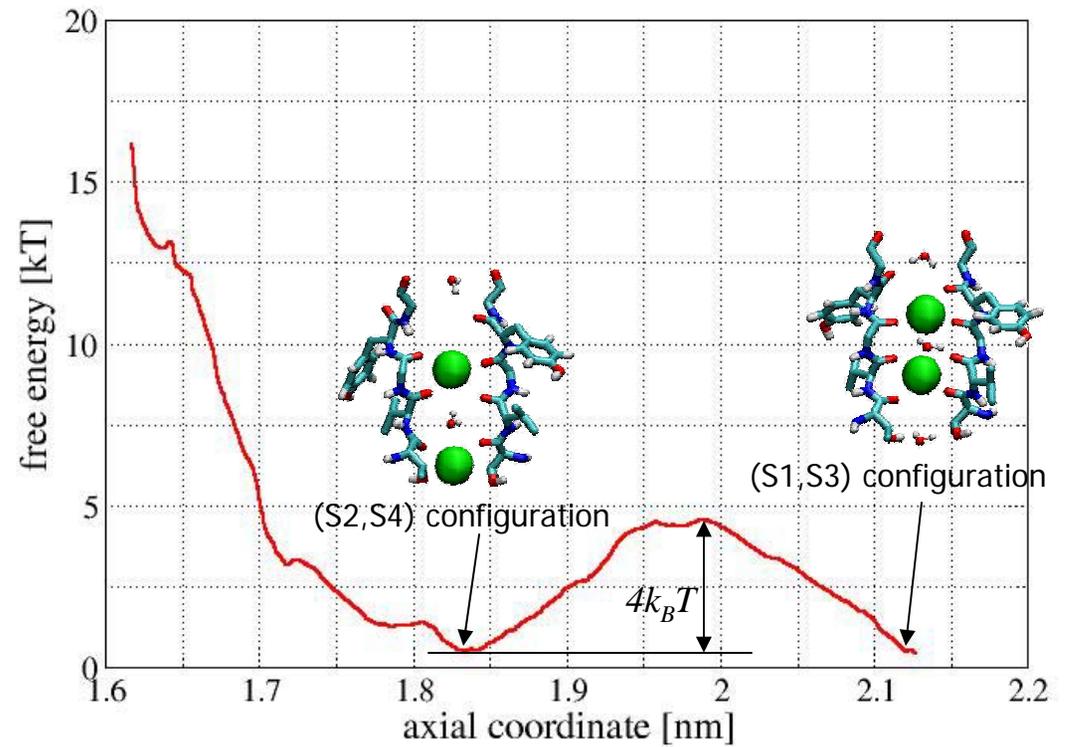
Results



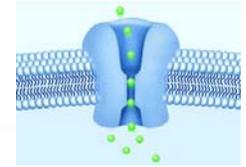
Free-energy profile determination



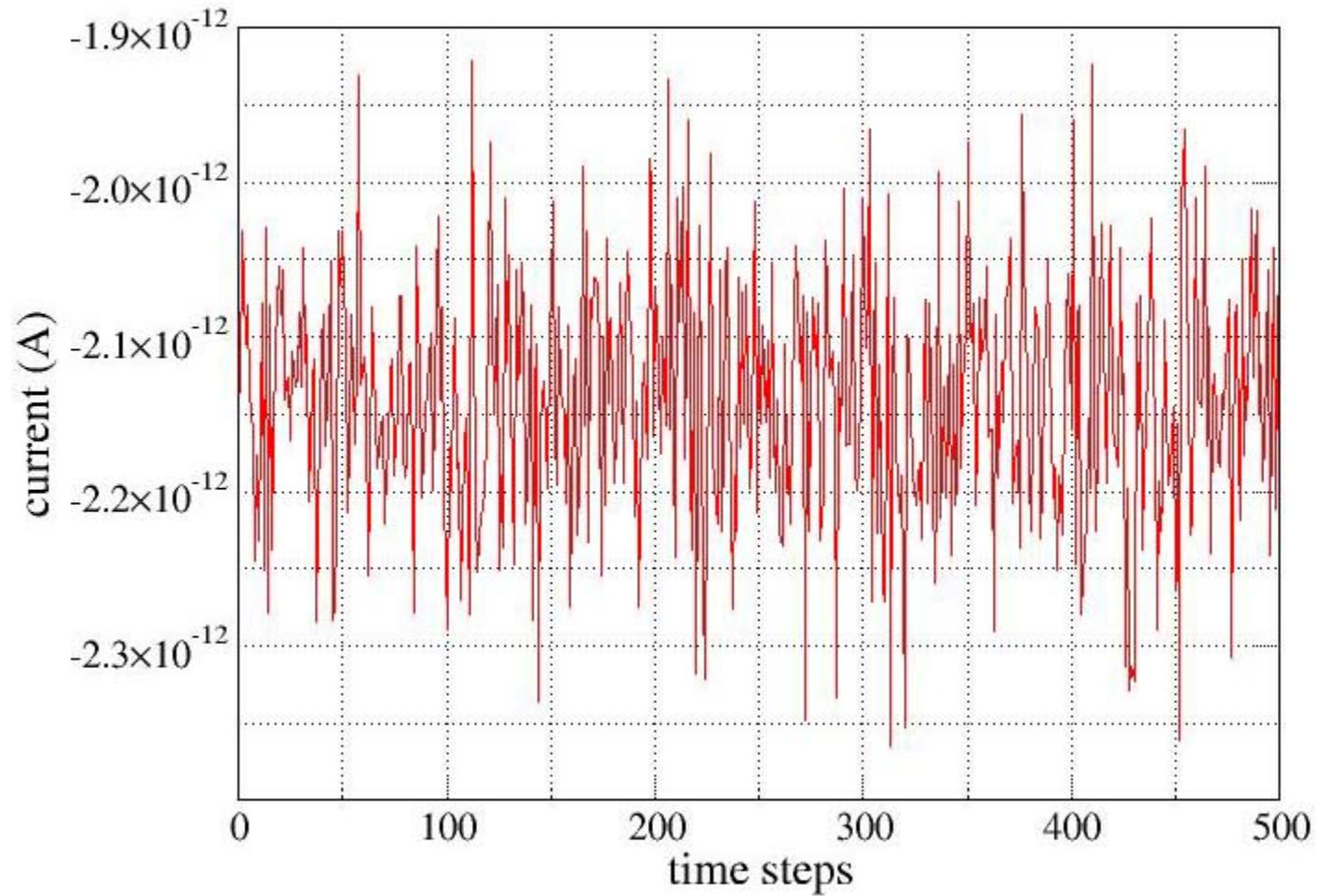
VMD movie



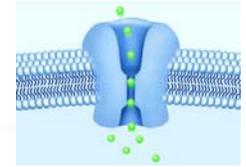
Results



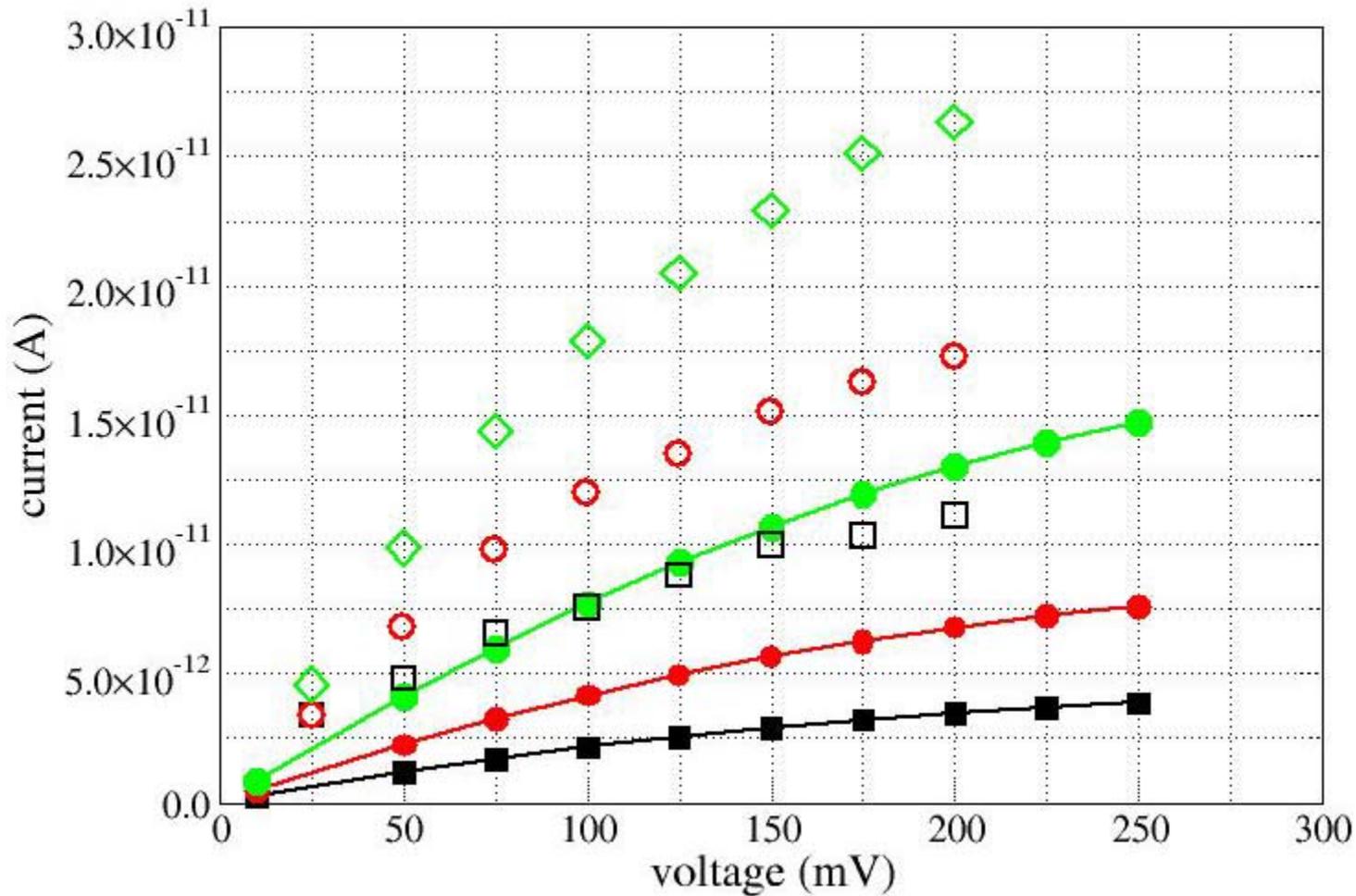
Current record from MC simulation



Results

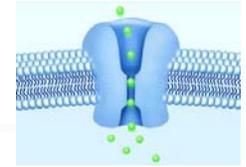


I-V characteristics

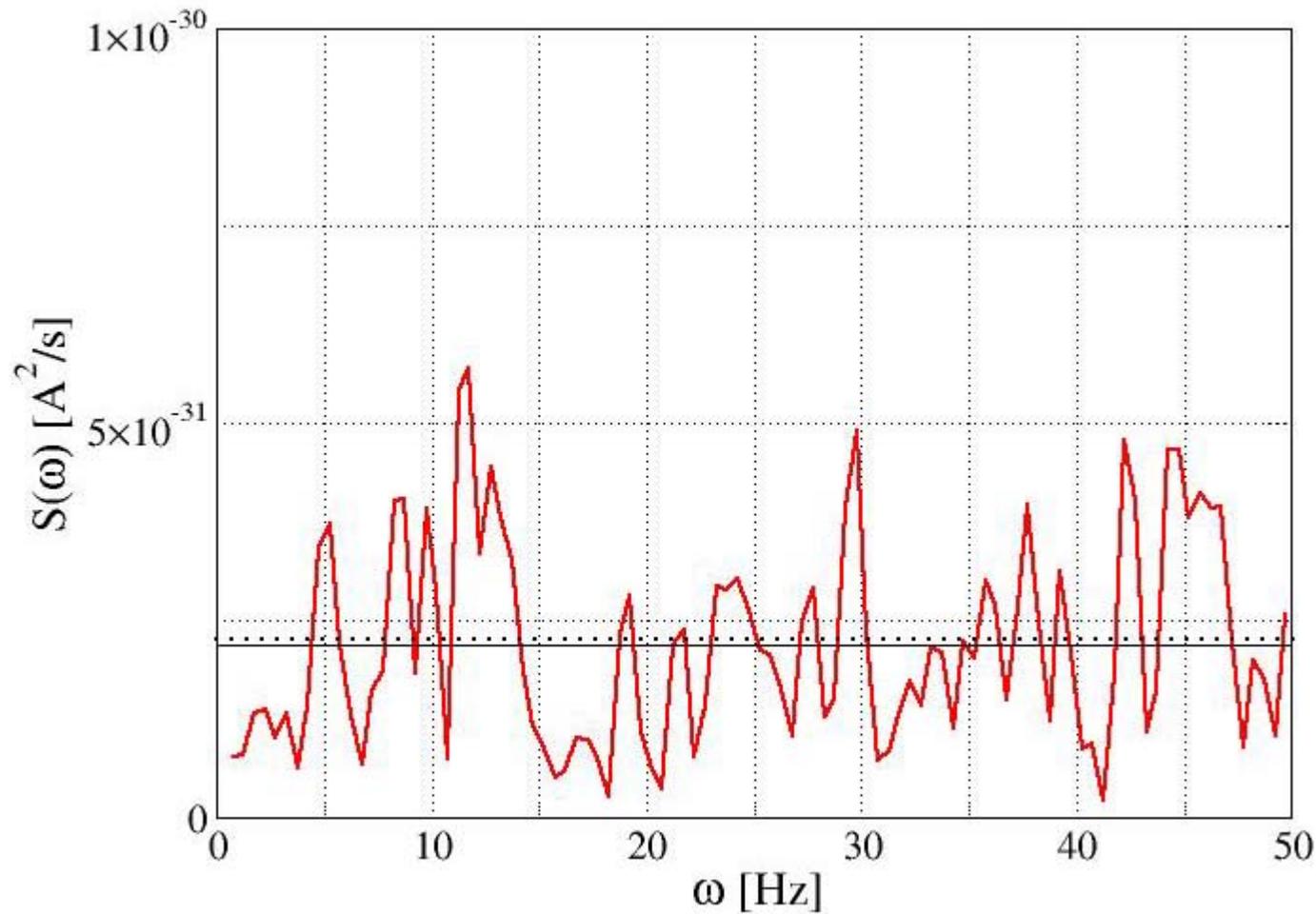


Experimental data from LeMasurier et al., *J. Gen. Physiol.*, **118** (3), 303 (2001)

Results



Noise Power Spectrum

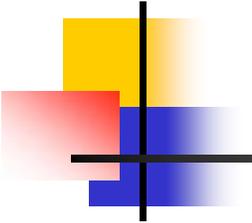


Theoretical value
(dots)

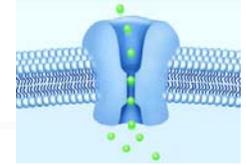
$2.27 \cdot 10^{-31} \text{ A}^2/\text{s}$

Calculated average
(line)

$2.18 \pm 0.13 \cdot 10^{-31} \text{ A}^2/\text{s}$



Further developments



- ✓ **Free-energy mapping** for all the relevant conduction paths
- ✓ **Analysis of noise** to identify possible correlations in ion exit
- ✓ Analysis of conduction properties in presence of gating
- ✓ Analysis of permeation properties of several group I ions (K, Na, Rb, ...)
- ✓ Analysis of other ion channels, with available structural conformation