## **TCAD** simulation of statistical variability

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#### Outline

- Introduction
- Sources of variability and TCAD challenges
  - Random discrete dopants
  - Line edge roughness
  - Poly-silicon gate granularity
  - Metal gate granularity
  - Statistical Reliability
- Examples
- Conclusion





### Variability Research in Europe

#### Modern

- MOdeling and DEsign of Reliable, process variation-aware Nanoelectronic devices, circuits and systems
- 31 partners in 9 European countries

#### Reality

- Reliable and Variability tolerant System-on-a-chip Design in More-Moore Technologies
- IMEC, STMicroelectronics, ARM, KU Leuven, U. Bologna, U. Glasgow

#### Trams

- Terascale Reliable Adaptive Memory Systems
- UP Catalunya, Intel, IMEC, U. Glasgow

#### Mordred

- Modelling of the reliability and degradation of next generation nanoelectronic devices
- Tampere U. of Tech., UCL, U. Glasgow, Vienna Inst. Micro., IMEC, Infineon, GSS, KU Leuven

#### NanoCMOS (UK)

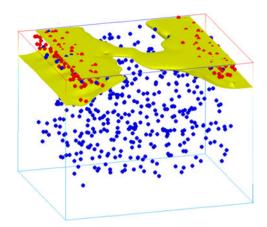
- Meeting the design challenges of nanoCMOS electronics
- U. Glasgow, U. Manchester, U. Southampton, U. York, U. Edinburgh, NeSC



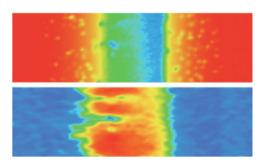


## Glasgow statistical 3D simulation tools

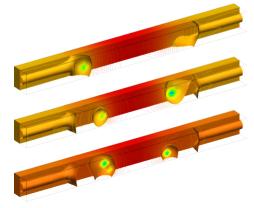
Drift-Diffusion (DD) with quantum corrections.



 Ensemble Monte Carlo (MC) with ab-initio impurity scattering.



Non-Equilibrium Green's Functions (NEGF).



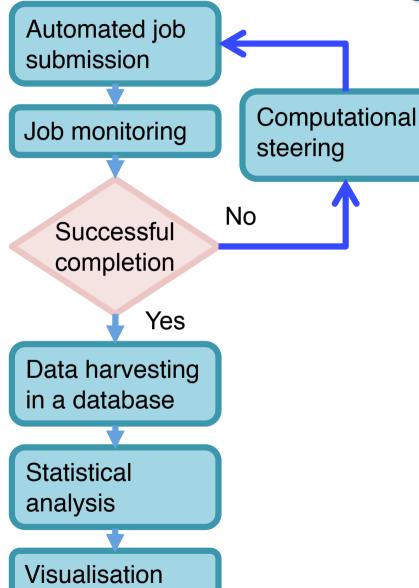




# Grid/cluster based simulation technology





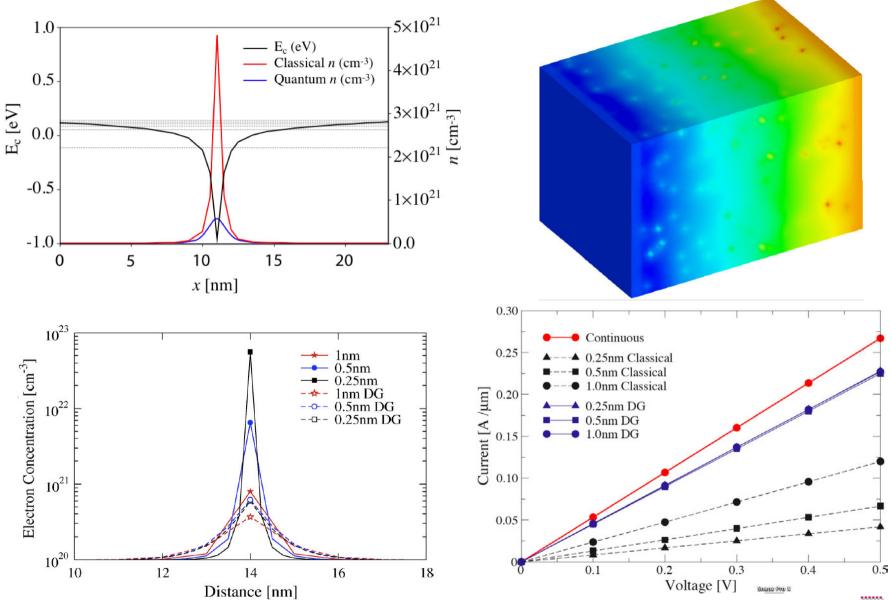








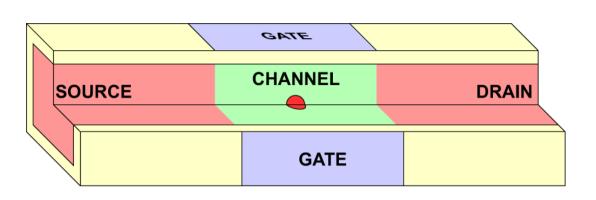
#### Quantum corrections using DG

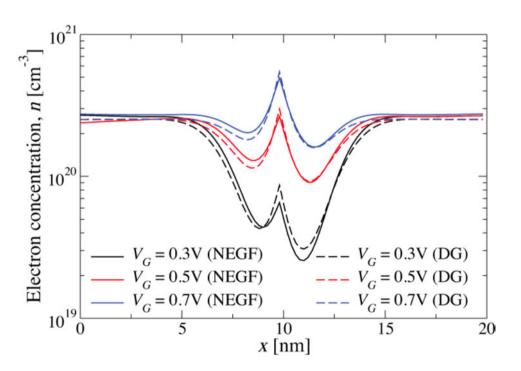


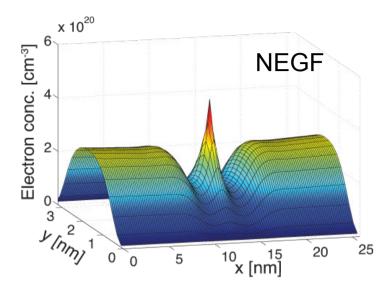


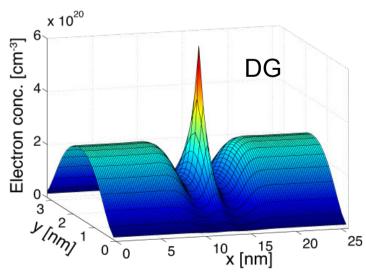
Simulation and Characterisation of Statistical CMOS Variability and Reliability SISPAD Workshop, Bologna 9/9/2010

#### How accurate is the DG solution?





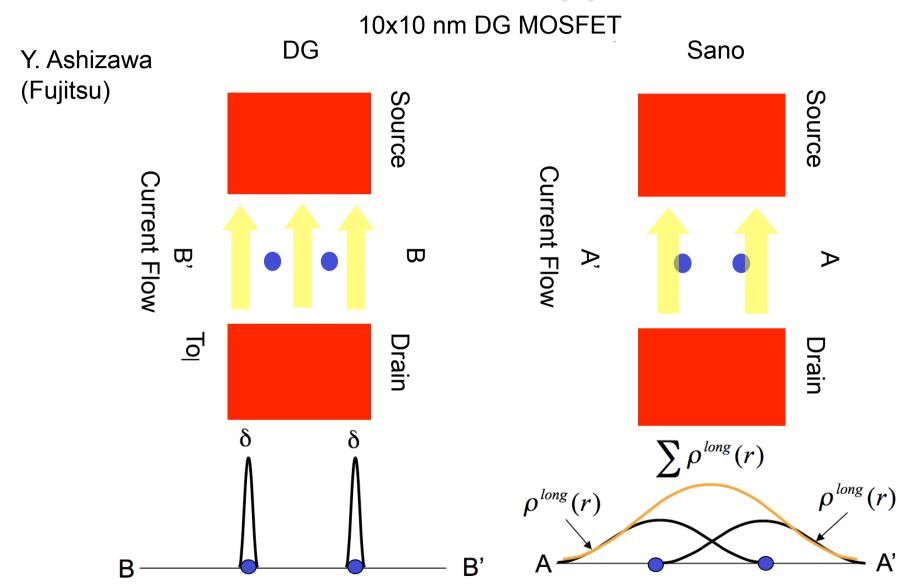








## DG vs. the Sano approach

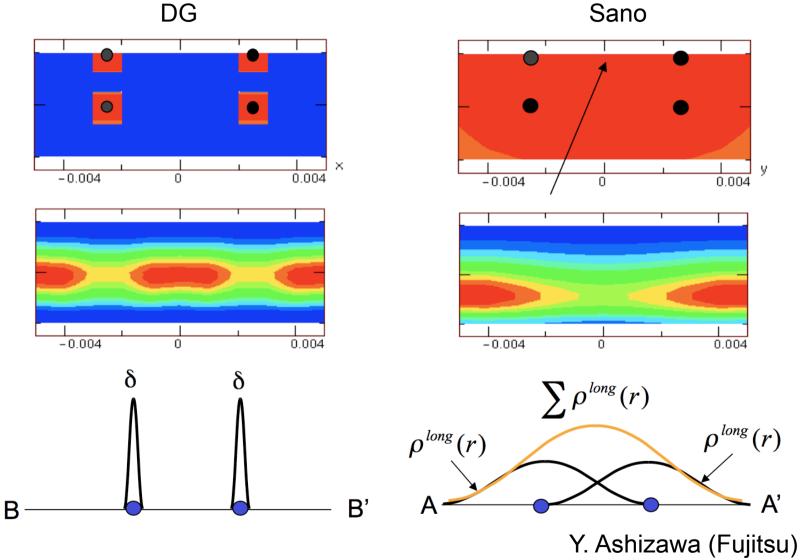






#### DG vs. the Sano approach

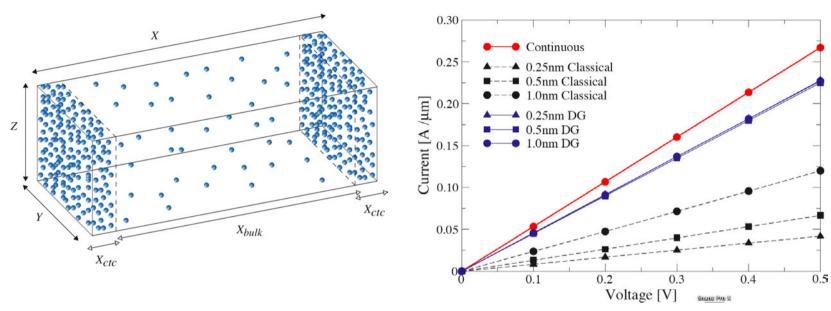
10x10 nm DG MOSFET







# The mobility dilemma (1) Doping concentration dependent mobility

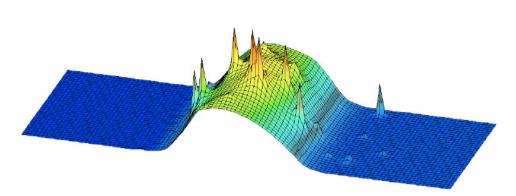


- The mobility is a statistical transport property.
- It has a meaning for sufficiently large self averaging system.
- No mobility can be assigned to individual dopants.
- Best solution is to use the continuous doping from which random dopants were generated.
- Even with DG corrections the resistance of an atomistic slab is larger compared to continuously doped one due to partial localization.

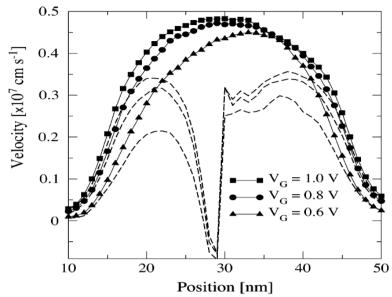




# The mobility dilemma (2) Velocity saturation, field dependence



Potential distribution in a MOSFET with random dopants



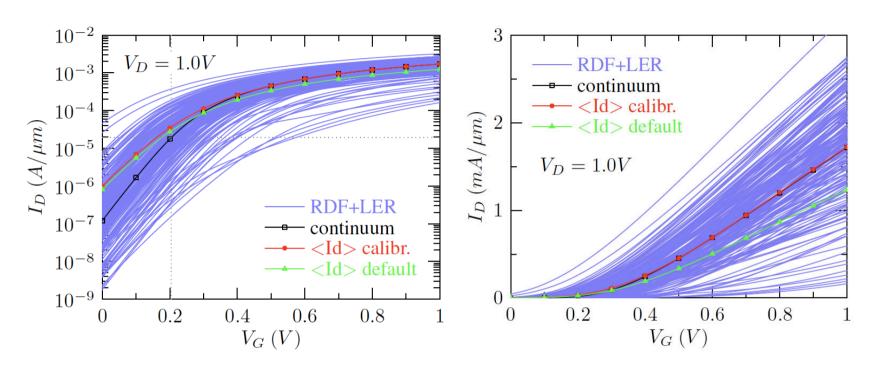
Velocity distribution in a MOSFET with single dopant

- □ Field dependent mobility has a meaning in 'adiabatic' conditions.
- The high electric field around single dopant cannot be used in the field dependent mobility model.
- The velocity saturation is associated with dissipative phonon scattering.
- The reduction of velocity around single dopant is associated with Coulomb scattering.





#### The calibration dilemma

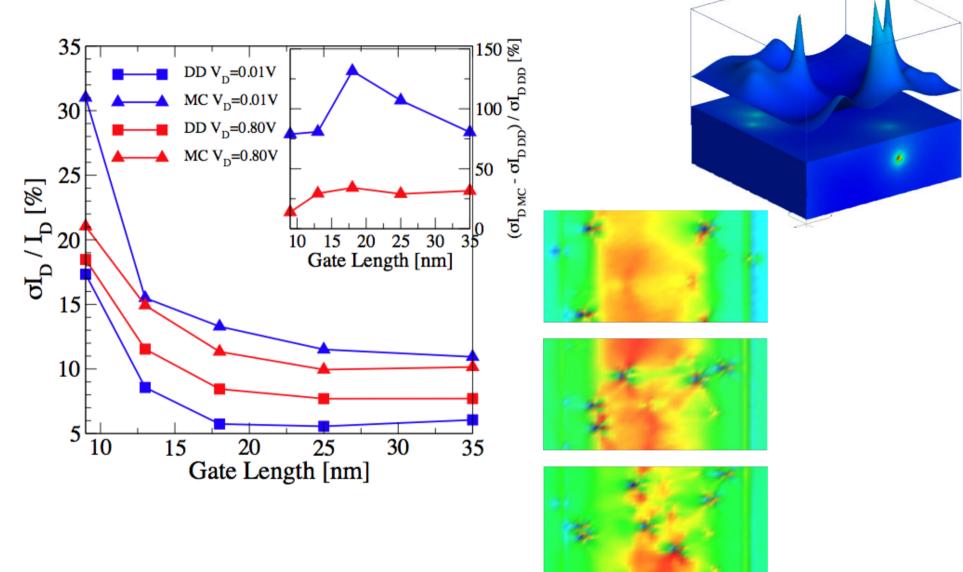


- The shape of the continuous simulation and the average 'atomistic'
   I-V curves are different.
- □ The calibration of continuous TCAD simulations to measurements which are equivalent to average atomistic simulation results in compensations through the mobility models..





Transport (scattering) related variability

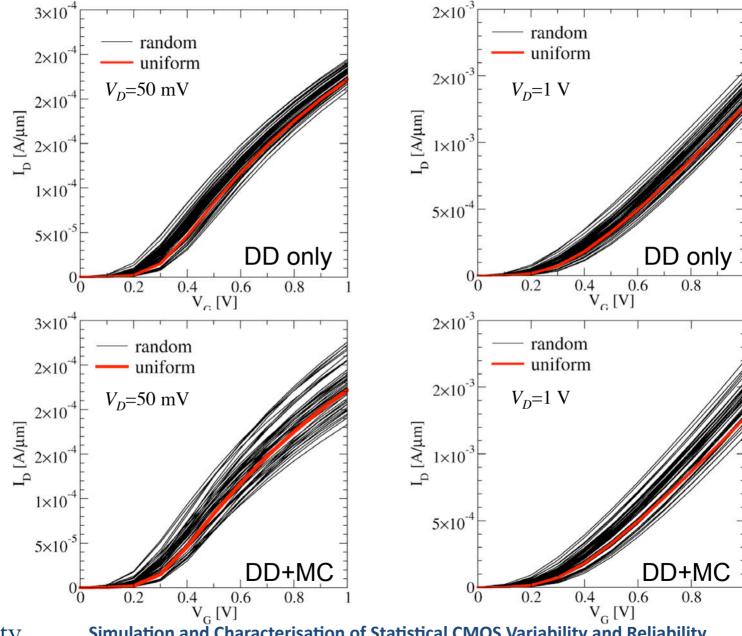






#### The impact of the transport related variability

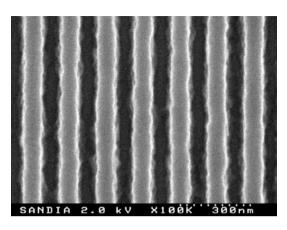
35 nm MOSFET



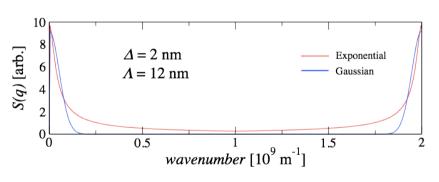


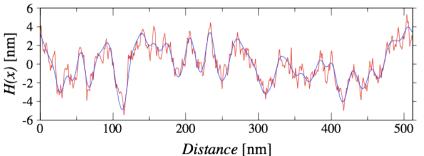


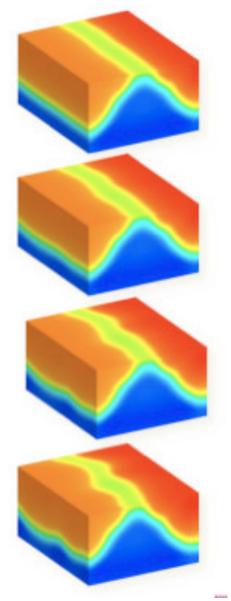
### LER is notoriously difficult to reduce



Sandia Labs - EUV



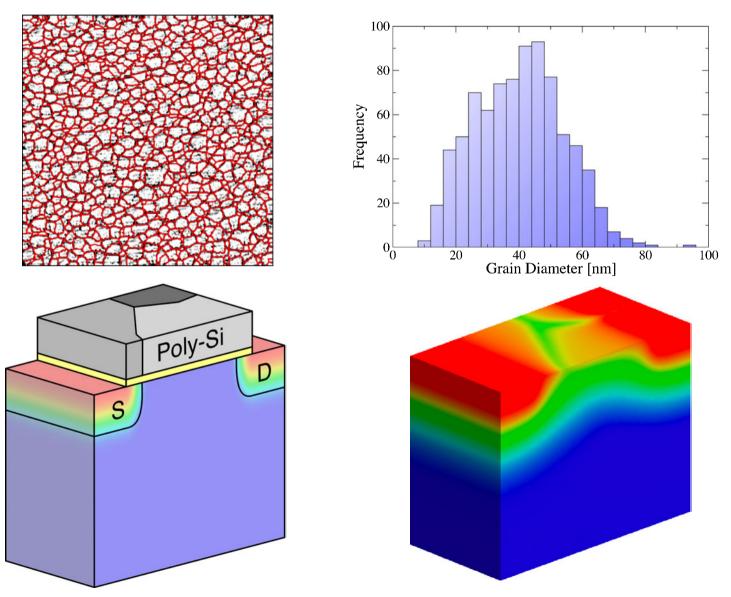








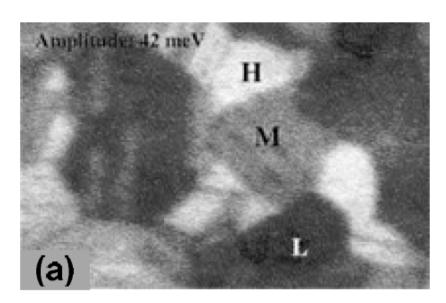
### **Poly-Silicon Grains**



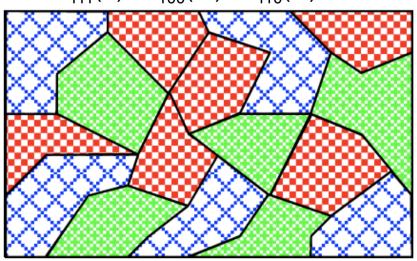


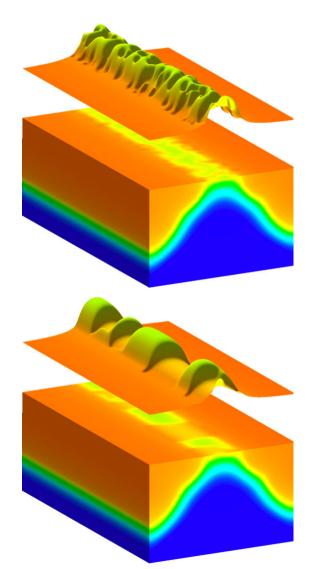


# Metal gate granularity (MGG)



$$\Phi_{111}(L)>\Phi_{100}(M)>\Phi_{110}(H)$$

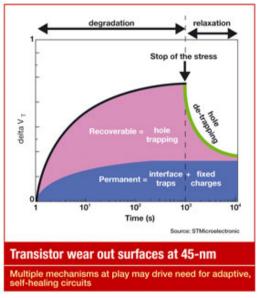


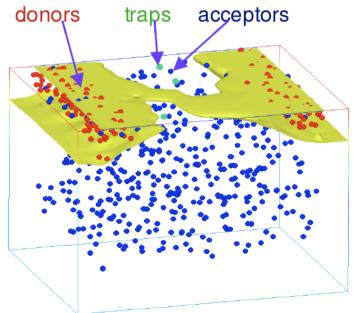


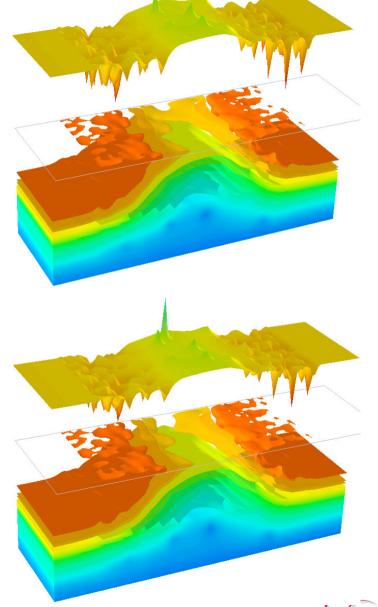




#### Statistical reliability: electrostatics



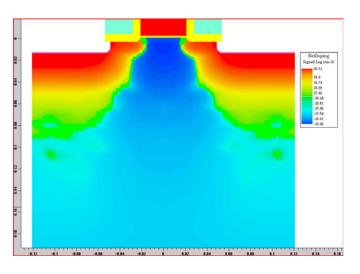


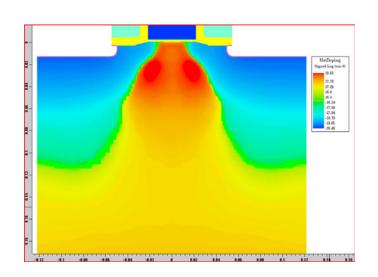


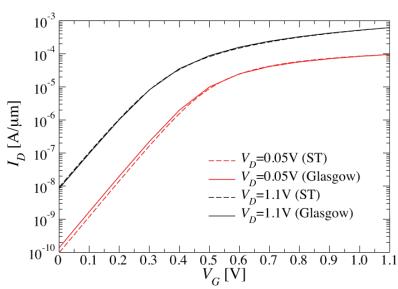


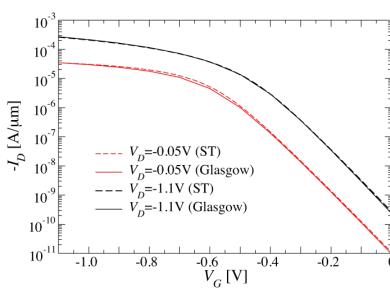
Simulation and Characterisation of Statistical CMOS Variability and Reliability SISPAD Workshop, Bologna 9/9/2010

# Example: 45nm Device Structure and Calibration





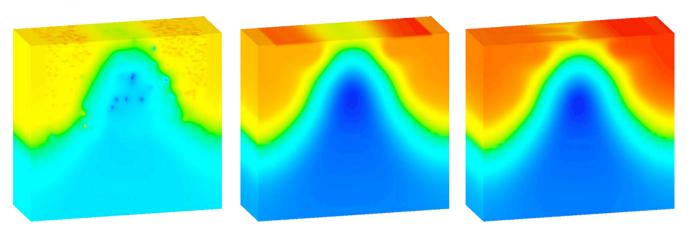








# Good agreement with measurements

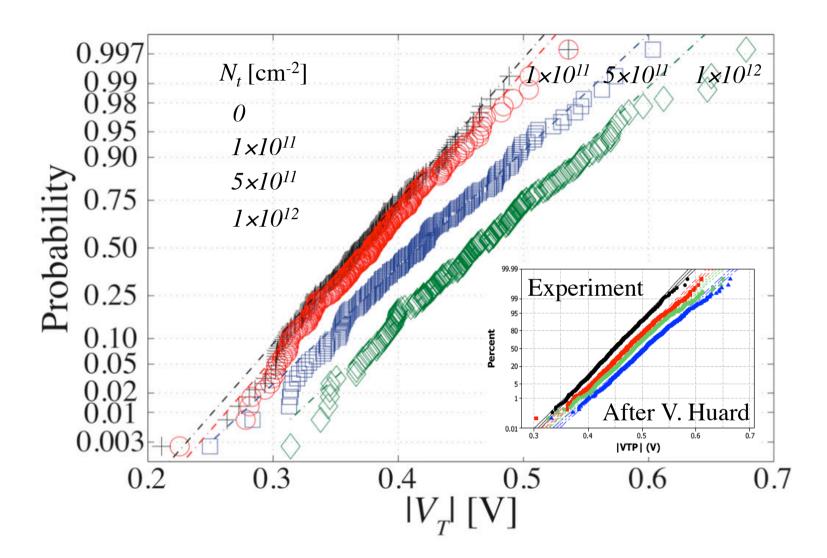


	<i>n</i> -channel	MOSFET	<i>p</i> -channel MOSFET		
	$\sigma V_T$ [mV]	$\sigma V_T$ [mV]	$\sigma V_T$ [mV]	$\sigma V_T$ [mV]	
	$(V_{DS}=0.05 \text{ V})$	$(V_{DS}=1.1 \text{ V})$	$(V_{DS}=0.05 \text{ V})$	(V <sub>DS</sub> =1.1 V)	
RDD	50	52	51	54	
LER	20	33	13	22	
PSG	30	26	-	-	
Combined	62	69	53	59	
Experimental	62	67	54	57	





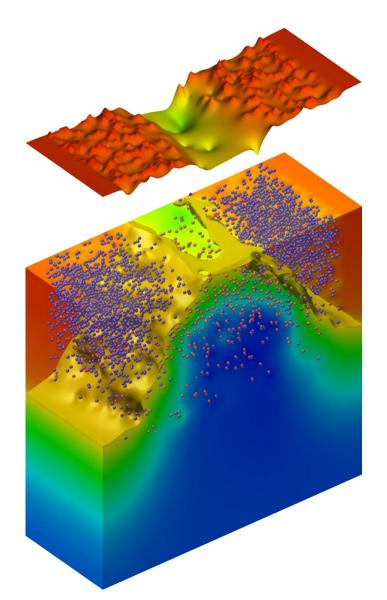
### Trapped charges (NBTI)

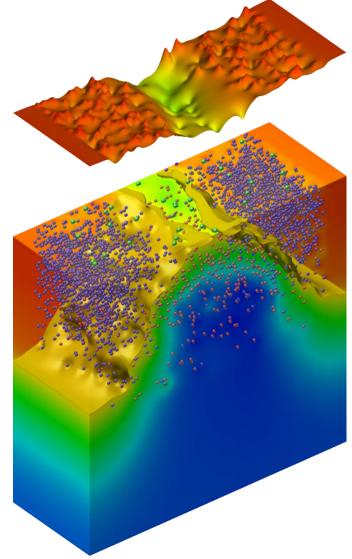






# Trapped charges (NBTI)

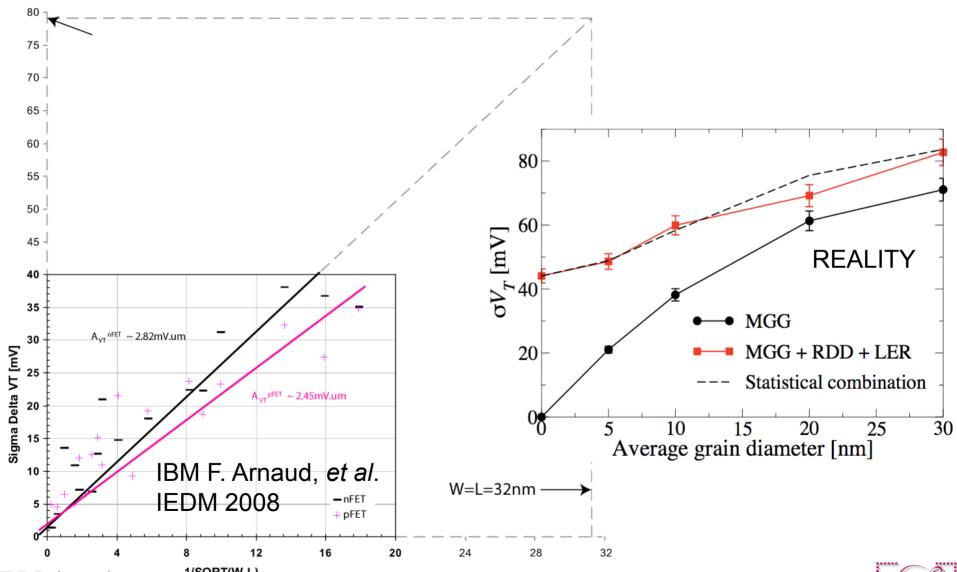








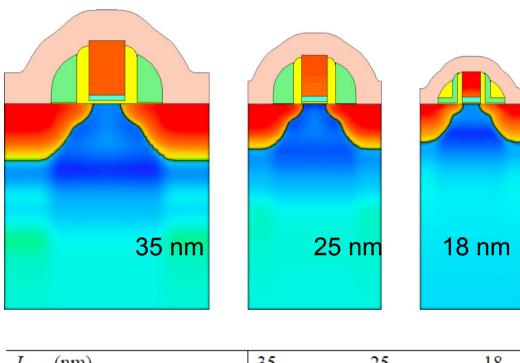
#### 32nm Metal Gate Granularity



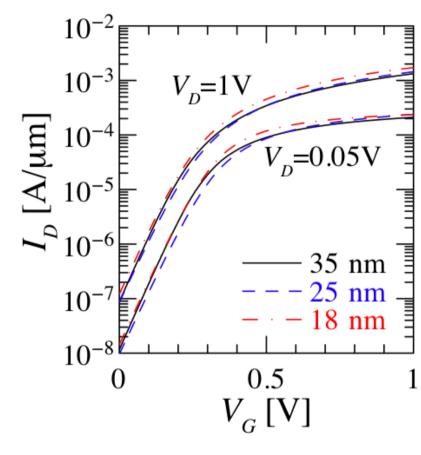




## Updated scaling – high-k/metal gate



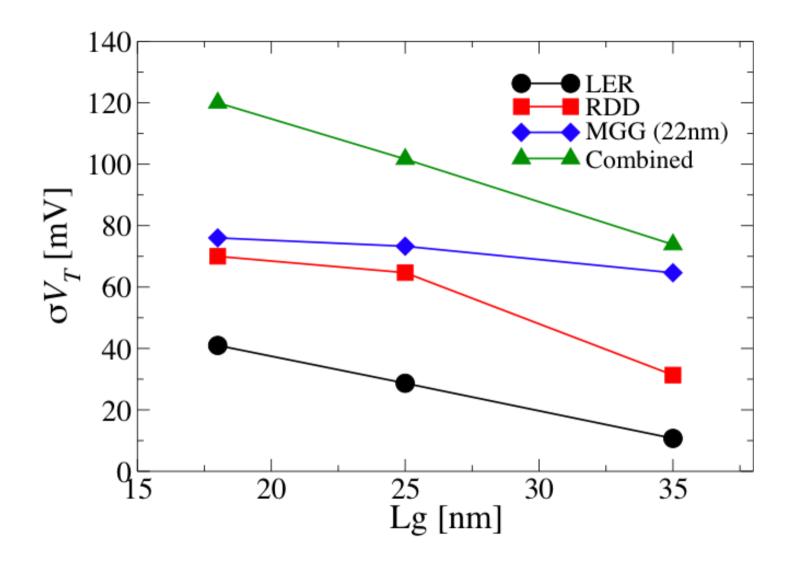
$L_{gate}$ (nm)	35	25	18
EOT (nm)	1.0	0.9	0.7
Stress liner thickness (nm)	30	22	15
Lateral length (nm)	200	130	100
$V_{dd}\left(\mathbf{V}\right)$	1.0	1.0	1.0







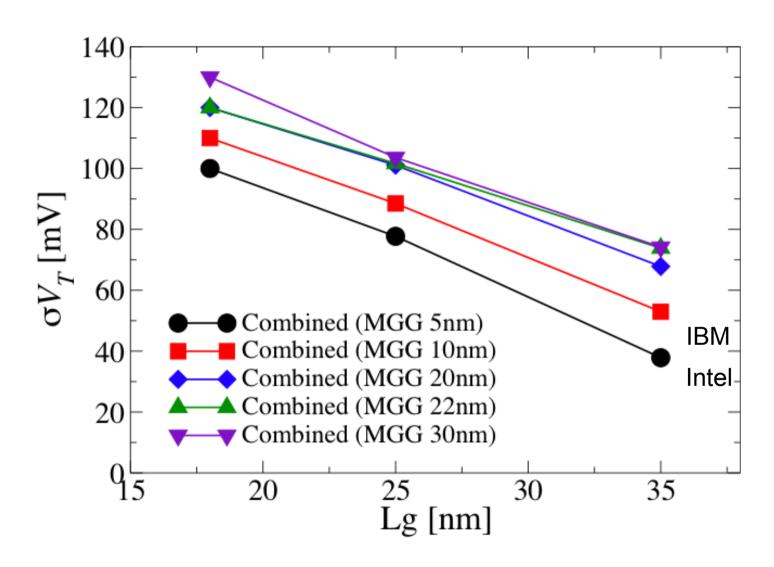
## Variability in high-k/metal gate MOSFETs







## Variability in high-k/metal gate MOSFETs





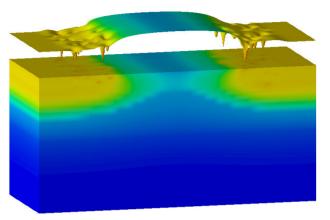


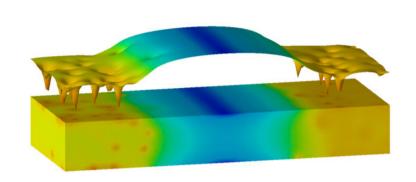


#### SOI and DG variability

32 nm FD SOI

22 nm DG



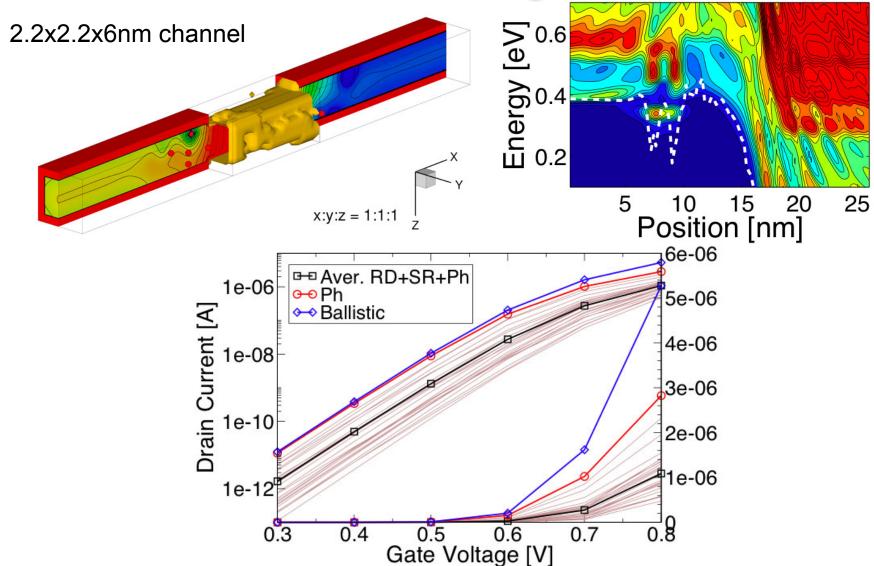


	$32$ nm $\sigma$	$V_T(mV)$	22nm σ	$V_T(mV)$
	$V_{ds}$ (50mV)	$V_{ds}(1.0V)$	$V_{ds}$ (50mV)	$V_{ds}$ (1.0V)
RDD	5.3	6.1	6.4	8.1
LER	3.3	8.6	5.8	13
Trap (1e11)	11	11	5.1	4.8
Trap (5e11)	24	25	13	12
Trap (1e12)	36	37	18	17
Combined (1e11)	13	15	10	16
Combined (5e11)	25	27	16	19
Combined (1e12)	37	38	20	23





# 3D NEGF simulator with variability and scattering







#### Conclusions

- There is a large amount of research being done in Europe on the study of variability and ways to deal with it in circuits and systems
- Underpinning this work are TCAD simulations which quantify the variability at a device level
- The major sources of statistical variability have been highlighted and some of the issues involved in including them in TCAD modelling have been discussed.



